



# Metaheuristics for Smart Manufacturing

## 1. Introduction

Thomas Weise · 汤卫思

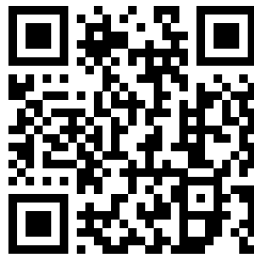
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- 1 Smart Manufacturing
- 2 Optimization Problems
- 3 Exact vs. Heuristic Algorithms
- 4 Summary and Outlook

The slides are available at <http://iao.hfuu.edu.cn/155>, the book at <http://thomasweise.github.io/aitoa>, and the source code at <http://www.github.com/thomasWeise/aitoa-code>

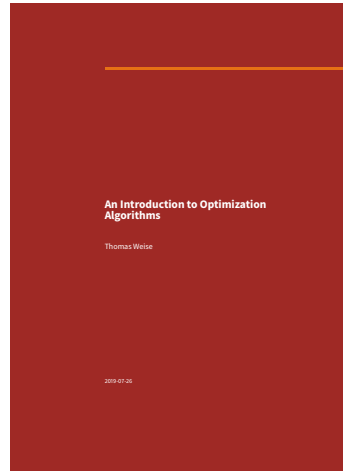


course book



course material

The contents of this course are available as free electronic book “*An Introduction to Optimization Algorithms*” <sup>[1]</sup> at <http://thomasweise.github.io/aitoa> in [pdf](#), [html](#), [azw3](#), and [epub](#) format, created with our [bookbildeR](#) tool chain.



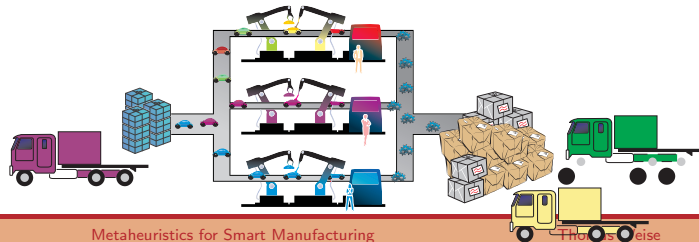
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# What is Smart Manufacturing?

## Smart Manufacturing<sup>[2]</sup>...

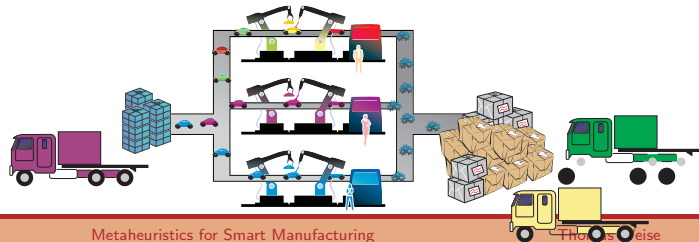
- has the goal of optimizing development, production, and logistics.



Intelligent Decisions  
by Intelligent Software

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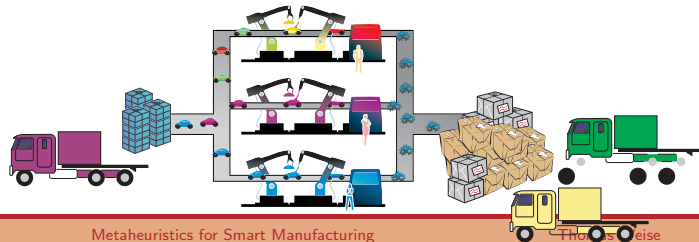
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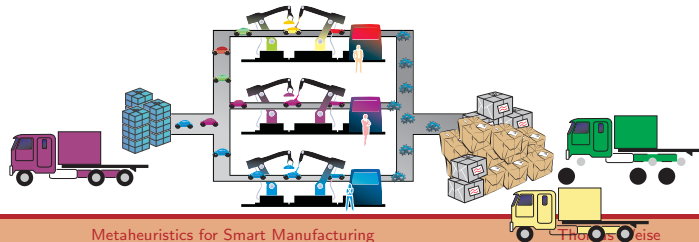
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- has the goal of optimizing development, production, and logistics.
- employs computer control and high levels of adaptability in the multi-phase process of creating a product from raw material.
- utilizes advanced information and manufacturing technologies to enable flexibility in production processes to address a dynamic market.
- requires increased workforce training for flexibility and use of the technology instead of simple repetitive tasks as in traditional manufacturing.



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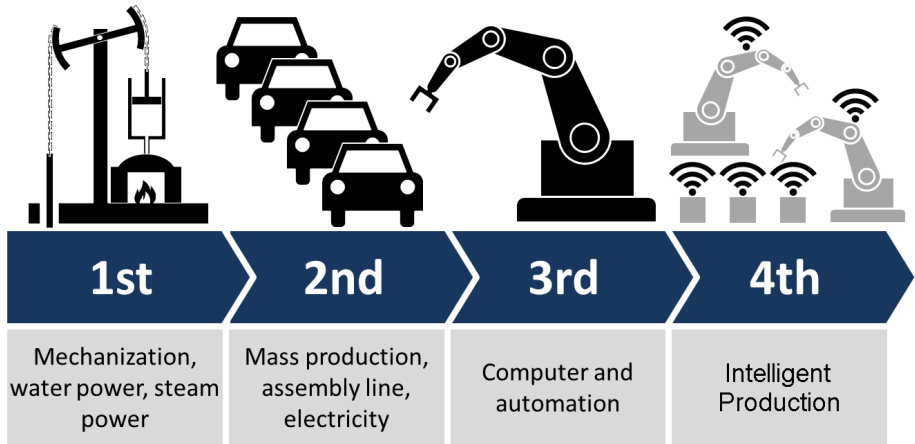


image source: modified from [http://en.wikipedia.org/wiki/File:Industry\\_4.0.png](http://en.wikipedia.org/wiki/File:Industry_4.0.png) <sup>[3]</sup>

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- **Computational Intelligence and Optimization** <sup>[1, 9, 10]</sup>: automatic intelligent decisions, automated planning, scheduling, design, management, . . .

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## What is optimization? <sup>[1, 9, 11]</sup>

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## What is optimization? [1, 9, 11]



What is the **cheapest** way to get from Hefei to Beijing?

## What is optimization? [1, 9, 11]



What is the **fastest** way for our team to finish all the work?

## What is optimization? [1, 9, 11]



How can I package these products using the **fewest** boxes?

## What is optimization? [1, 9, 11]



What is the **fastest** way to lose 20kg?

## What is optimization? <sup>[1, 9, 11]</sup>

### Definition (Optimization Problem: Economical View)

An optimization problem is a situation which requires deciding for one choice from a set of possible alternatives in order to reach a predefined/required benefit at minimal costs.

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### Definition (Optimization Problem: Simplified Mathematical View)

Solving an optimization problem requires finding an input value  $y^* \in \mathbb{Y}$  from a set  $\mathbb{Y}$  of allowed values for which a mathematical function  $f : \mathbb{Y} \mapsto \mathbb{R}$  takes on the smallest possible value.

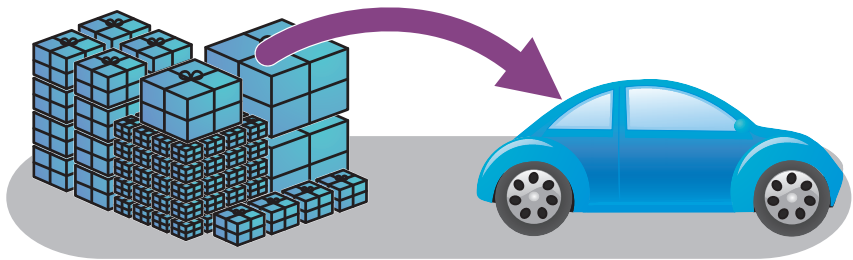
- Many questions in the real world are *optimization problems*

- Many questions in the real world are *optimization problems*, e.g.,
  - Find the *shortest* tour for a salesman to visit a certain set of cities in China and return to Hefei!

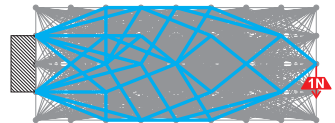
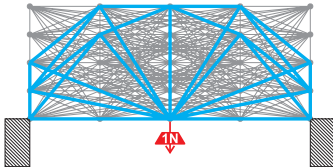
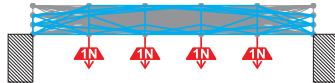
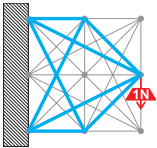




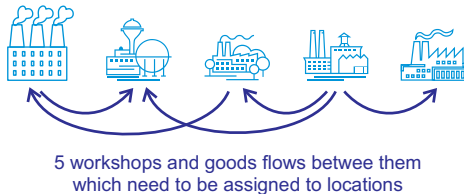
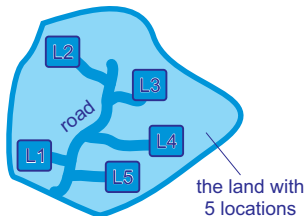
- Many questions in the real world are *optimization problems*, e.g.,
  - Find the *shortest* tour for a salesman to visit a certain set of cities
  - I need to transport  $n$  items from here to another city but they are too big to transport them all at once. How can I load them best into my car so that I have to travel back and forth the least times?



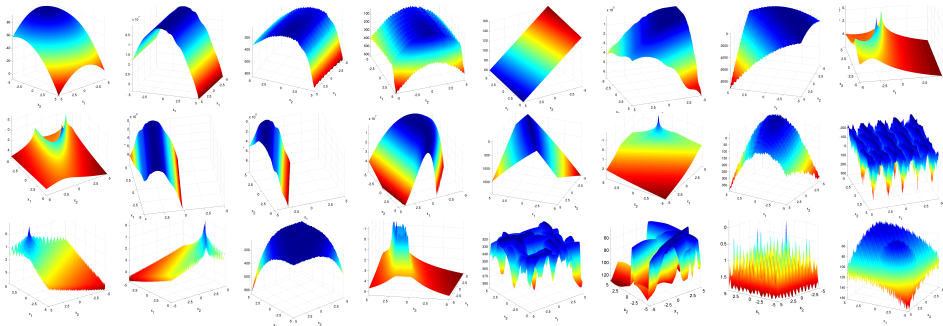
- Many questions in the real world are *optimization problems*, e.g.,
  - Find the *shortest* tour for a salesman to visit a certain set of cities
  - I need to transport  $n$  items from here to another city
  - How can I construct a truss which can hold a certain weight with at most a certain amount of iron?



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  - I need to transport  $n$  items from here to another city
  - Construct a truss which can hold a certain weight
  - I want to build a large factory with  $n$  workshops. I know the flow of material between each two workshops and now need to choose the locations of the workshops such that the overall running cost incurred by material transportation is *minimized*.



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  - Find the *shortest* tour for a salesman to visit a certain set of cities
  - I need to transport  $n$  items from here to another city
  - Construct a truss which can hold a certain weight
  - Assign workshops to locations
  - Find the minima of complex, multi-dimensional mathematical formulas



- Let us now look at a more complex example from the field of transportation planning.

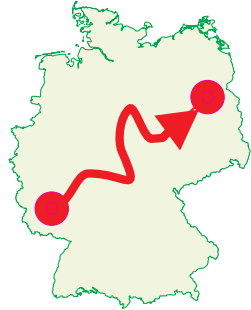
- Let us now look at a more complex example from the field of transportation planning.
- This was an actual project for a major German logistics company

- Build a system which tells a logistics company what it needs to do to fulfill all transportation orders at minimum costs. <sup>[12–16]</sup>

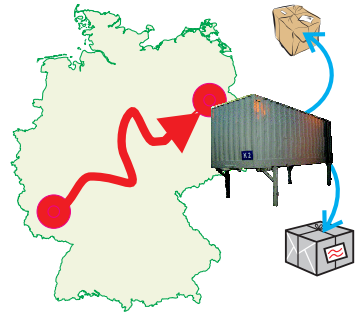
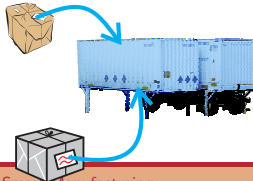
- Build a system which tells a logistics company what it needs to do to fulfill all transportation orders at minimum costs. <sup>[12–16]</sup>
- What does this mean?



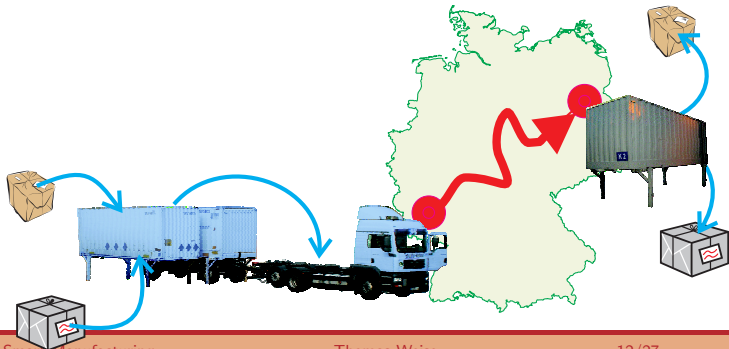
- Build a system which tells a logistics company what it needs to do to fulfill all transportation orders at minimum costs. <sup>[12–16]</sup>
  - ① Find routes on the map



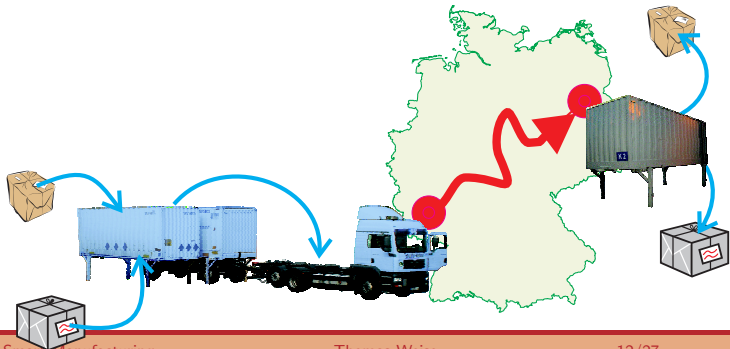
- Build a system which tells a logistics company what it needs to do to fulfill all transportation orders at minimum costs. <sup>[12–16]</sup>
  - ① Find routes on the map and assignments of orders to containers



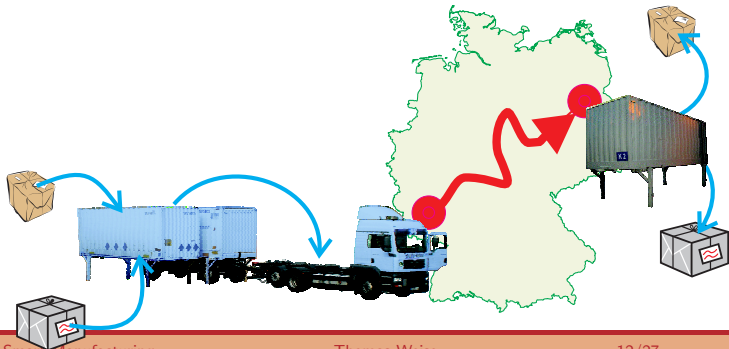
- Build a system which tells a logistics company what it needs to do to fulfill all transportation orders at minimum costs. <sup>[12–16]</sup>
  - ① Find routes on the map and assignments of orders to containers and containers to trucks



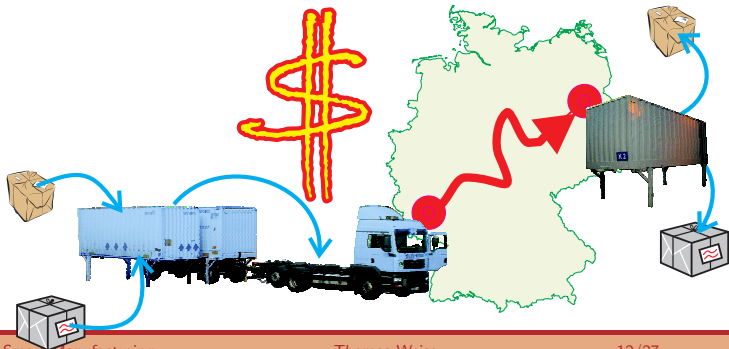
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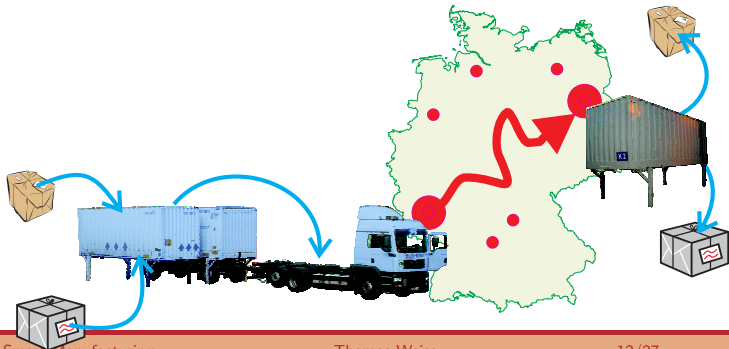
- Build a system which tells a logistics company what it needs to do to fulfill all transportation orders at minimum costs. <sup>[12–16]</sup>
  - ① Find routes on the map and assignments of orders to containers and containers to trucks/trains which minimize the undelivered orders



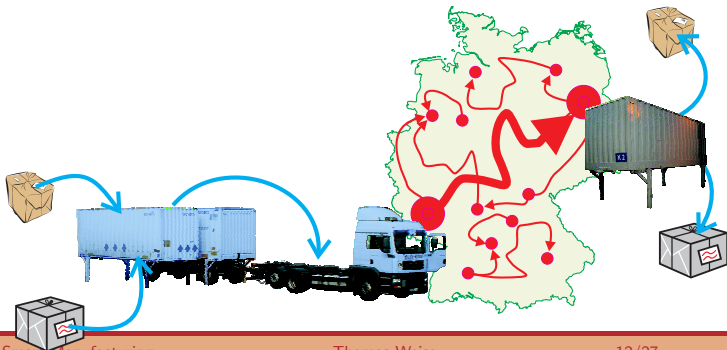
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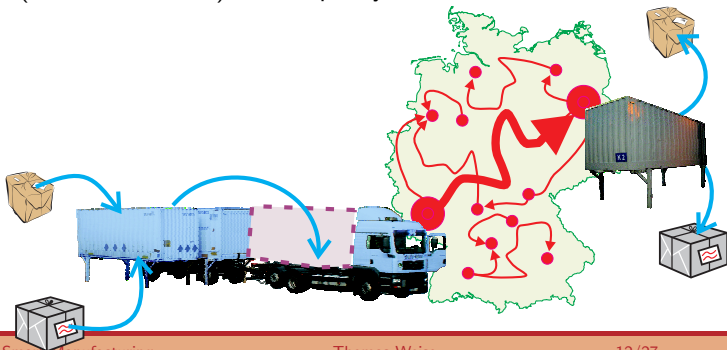


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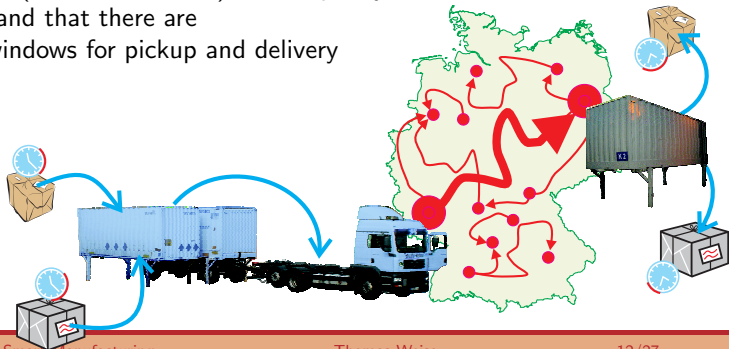




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  - ⑥ Time limit for optimization: 1 day

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- In this course, you will learn how we can do such a thing.

- So how is all of this related to smart manufacturing?

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- No enterprise can waste money

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- All kinds of the previously mentioned problems can occur in manufacturing.
- For example, logistics exist inside and outside a company, and even on the factory floor!

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optimization  
operations research  
computational intelligence  
machine learning  
data mining

delivery

production

management

products /  
services

sales

- optimized logistics (business-to-customer)
  - planning and scheduling of maintenance visits
  - planning and scheduling of supply visits
- production planning and scheduling
  - optimized assignment of jobs/orders to machines
  - optimization of production processes
  - optimization of stock-keeping
  - optimization of intra-enterprise logistics
  - optimization of supply chains
  - optimization of factory layouts and intra-factory logistics
- scheduling of employee work
- optimal assignment of employees to tasks or customers
- optimized locations for new branch offices  
(based current or predicted future customers)
- optimization of product design
- optimization of product feature configuration
- optimization of service offers
- improved tailoring of products/services to customers
- optimization of pricing and offers
- mining of customer data for targeted offers

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- We focus only on the first of the two issues: optimization algorithms and their implementation.

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- 4 Summary and Outlook

- In optimization, there exist *exact* and *heuristic* algorithms.



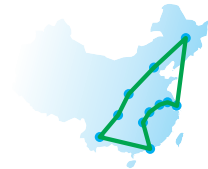
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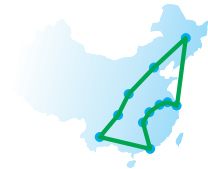
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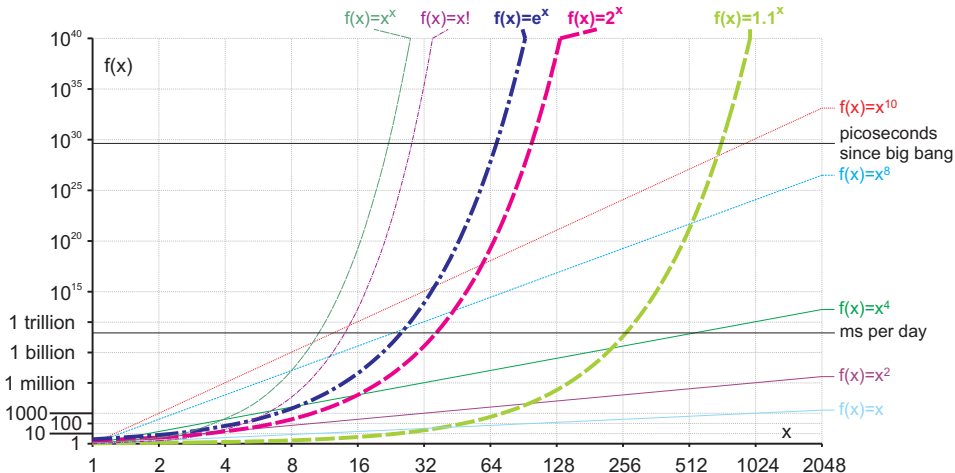


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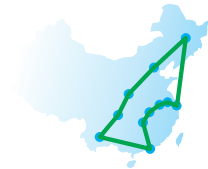


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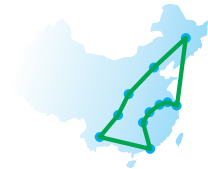


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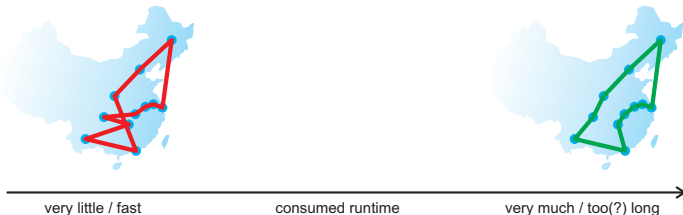
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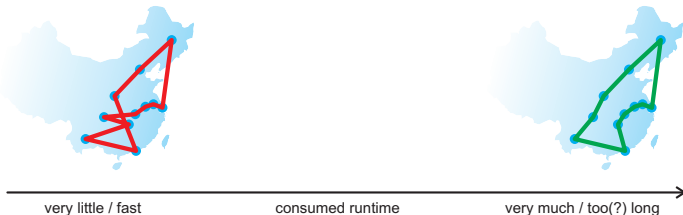
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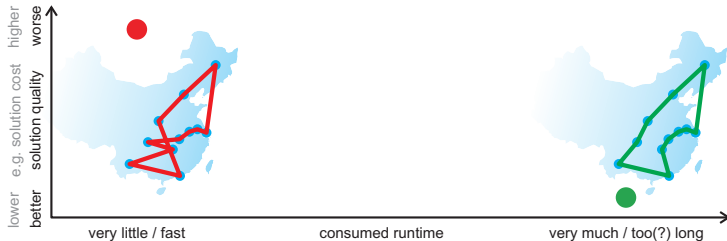




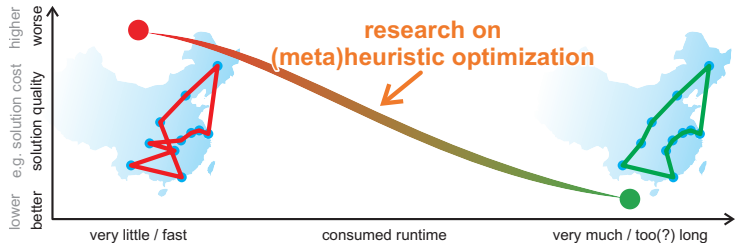
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- However, there are many different optimization problems and often we won't see a “pure” TSP in practice, there usually will be additional constraints and restrictions or multiple cars etc.

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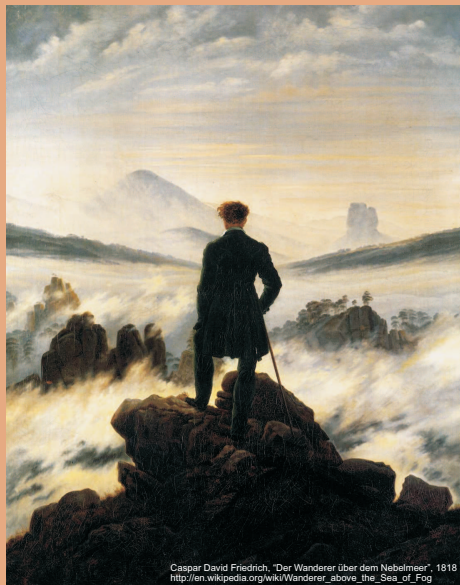
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- The goal is to be able to recognize and identify optimization problems as they occur in many fields, especially in Intelligent Manufacturing scenarios, and to develop basic algorithms to solve them.

# 谢谢

## Thank you

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